

[Technical Calculations] Selection of Single Axis Actuator (2)

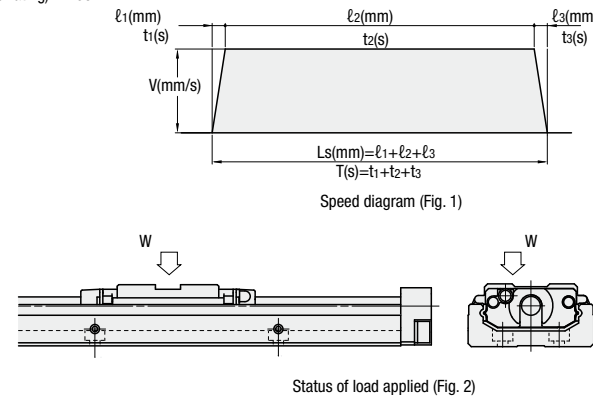
Selection is easy with Single Actuator calculation tool available at:
http://fawos.misumi.jp/FA_WEB/unit_en/web/misumi_LX_sg.html

Rated lifetime calculation example

1 Model number for examination

Operating conditions : LX26
 Rail : C (Basic dynamic load rating)=6522N Co (Basic static load rating)=11871N
 Ball screw : Ca (Basic dynamic load rating)=1712N Coa (Basic static load rating)=2251N
 Support bearings : Ca (Basic dynamic load rating)=1637N Poa (Basic static load rating)=1205N

Load mass : 10kg
 Maximum speed : 250mm/s
 Acceleration : 833mm/s²
 Stroke : 200mm
 Gravity : g=9.81m/s²
 Position : Horizontal
 Speed diagram : (Fig. 1)
 Operating Conditions : (Fig. 2)



2 Examination

Temporary selection

Use a travel distance of 200 mm with an acceleration of 833 mm/s² and a maximum speed of 250 mm/s. Based on these conditions, assume that the LX26 series is used. (The selection software can be used on the Misumi website after customer registration has been completed.)

3 Calculation

3-1 Examination of rail

Multiply the moment equivalent coefficient in the table with the load according to the condition in which one nut block is used.

Load for nut block

- At constant speed
 $F_{e1} = Y_v F_v = Y_v \cdot W \cdot g = 1 \cdot 10 \cdot 9.81 = 98.1 \text{ (N)}$
- At acceleration
 $F_{e2} = Y_v F_v + Y_p K_p M a = 0.5 \cdot 98.1 + 1 \cdot 0.17 \cdot 70 \cdot 0 = 60.95 \text{ (N)}$
- At deceleration
 $F_{e3} = Y_v F_v + Y_p K_p M a = 0.5 \cdot 98.1 + 1 \cdot 0.17 \cdot 70 \cdot 0 = 60.95 \text{ (N)}$

Static safety coefficient

$$f_s = \frac{C_o}{F_{max}} = \frac{C_o}{W \cdot g} = \frac{11871}{98.1} = 121.1$$

Rated life span

Axial average load

$$F_m = \sqrt[3]{\frac{1}{L_s} (F_{e1}^3 \cdot L_1 + F_{e2}^3 \cdot L_2 + F_{e3}^3 \cdot L_3 \cdot F_{en}^3 \cdot L_n)} = 87.72 \text{ (N)}$$

Rated life span

$$L = \left(\frac{C}{f_w \cdot F_m} \right)^3 \times 50 = 11.89 \times 10^6 \text{ km}$$

fw: Load coefficient 1.2
La: Travel distance 50(km)

3-2 Examination of ball screw

Obtain the axial loads for the parts and the average load from the speed diagram.

Lifetime of ball screw

Axial load

- At constant speed
 $F_{e1} = \mu \cdot W \cdot g = 0.01 \times 10 \times 9.81 = 0.981 \text{ (N)}$
- At acceleration
 $F_{e2} = F_{e1} + W \cdot a \times 10^{-3} = 0.981 + 10 \cdot 0.833 = 9.311 \text{ (N)}$
- At deceleration
 $F_{e3} = F_{e1} - W \cdot a \times 10^{-3} = 7.352 \text{ (N)}$

Static safety coefficient

$$f_s = \frac{C_{oa}}{F_{max}} = \frac{C_{oa}}{F_{e2}} = \frac{2251}{9.311} = 241.76$$

Buckling load

$$P_1 = \frac{n \cdot \pi^2 \cdot E \cdot I}{\ell a^2} \times 0.5 = 5562.02 \text{ (N)}$$

P₁ : Buckling load
 ℓa : Distance between mounting points 250(mm)
 E : Young's modulus 2.06×10⁵(N/mm²)
 n : Coefficient according to mounting method
 0.5: Safety factor
 I : Minimum geometrical moment of inertia of screw shaft

$$I = \frac{\pi \cdot d_1^4}{64} = 85.49 \text{ (mm}^4\text{)}$$

d₁ : Root diameter of screw shaft 6.46(mm)

Allowable tension/compression load

$$P_2 = \frac{\delta \cdot \pi \cdot d_1^2}{4} = 4818.06$$

P₂ : Allowable tension/compression load (N)
 δ : Allowable tension/compression stress 147(N/mm²)
 d₁ : Root diameter of screw shaft 6.46(mm)

Critical speed

$$N_1 = \frac{60 \cdot \lambda^2}{2\pi \cdot \ell b^2} \cdot \sqrt{\frac{E \times 10^3 \cdot I}{\gamma \cdot A}} \times 0.8 = 12485 \text{ (min}^{-1}\text{)}$$

N₁ : Critical speed
 ℓb : Distance between mounting points
 E : Young's modulus 2.06×10⁵(N/mm²)
 λ : Coefficient according to mounting method (Fixed-Support 3.927)
 γ : Density (7.85×10⁻⁶kg/mm³)
 0.8: Safety factor

DN value

$$DN = 62250 (\leq 70000)$$

D : Ball center to center diameter (8.3mm)
 N : Maximum number of operating revolutions (min⁻¹)

LX2602	Rail	Ball screw	Support bearing
Static safety factor	121.1	241.76	129.42
Buckling load (N)	-	5562.02	-
Allowable tension/compression load (N)	-	4818.06	-
Critical speed (min ⁻¹)	-	12485	-
DN value	-	62250	-
Rated lifetime (km)	11.89×10 ⁶	22.31×10 ⁶	19.505×10 ⁶
Maximum axial load (N)	-	9.311	-
Maximum number of operating revolutions	-	7500	-

Rated life span

Axial average load

$$F_m = \sqrt[3]{\frac{1}{L_s} (F_{e1}^3 \cdot L_1 + F_{e2}^3 \cdot L_2 + F_{e3}^3 \cdot L_3 \cdot F_{en}^3 \cdot L_n)} = 6.096 \text{ (N)}$$

Rated life span

$$L = \left(\frac{C_a}{f_w \cdot F_m} \right)^3 \cdot \ell \times 10^6 = 25.64 \times 10^6 \text{ (km)}$$

fw : Load coefficient 1.2
 ℓ : Ball screw lead 2 (mm)

3-3 Examination of support bearing

Axial load

F_{e1}=0.981(N)
 F_{e2}=9.311(N)
 F_{e3}=7.352(N)

Static safety coefficient

$$f_s = \frac{P_{oa}}{F_{max}} = \frac{P_{oa}}{F_{e2}} = 129.42$$

Equivalent load

Axial average load

$$F_m = \sqrt[3]{\frac{1}{L_s} (F_{e1}^3 \cdot L_1 + F_{e2}^3 \cdot L_2 + F_{e3}^3 \cdot L_3 \cdot F_{en}^3 \cdot L_n)} = 6.096 \text{ (N)}$$

Rated lifetime

$$L = \left(\frac{C_a}{f_w \cdot F_m} \right)^3 \cdot \ell \times 10^6 = 22.41 \times 10^6 \text{ (km)}$$

fw : Load coefficient 1.2
 ℓ : Ball screw lead 2 (mm)